# **Another Look at SSIM Image Quality Metric**

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## Abstract

We review the design of the SSIM quality metric and offer an alternative model of SSIM computation, utilizing subband decomposition and identical distance measures in each subband. We show that this model performs very close to the original and offers many advantages from a methodological standpoint. It immediately brings several possible explanations of why SSIM is effective. It also suggests a simple strategy for band noise allocation to improve SSIM scores. This strategy may aid the design of encoders or preprocessing filters for video coding. Finally, this model leads to more direct mathematical connections between SSIM, MSE, and SNR metrics, improving previously known results

#### 1. Introduction

The Structural Similarity (SSIM) metric [1,2] has been around for nearly two decades and has become one of the most established and frequently used metrics for image and video quality analysis. Many research papers have followed, extending SSIM in multiscale, 3D, and temporal dimensions [3-6], analyzing its mathematical properties [7-9], and discussing its applications for improving the design of encoding algorithms [10-13] and streaming systems [14-16].

Yet, despite all the progress and broad acceptance in practice, what SSIM means from a physical, mathematical, and signal processing standpoint is not entirely understood. The original papers [1,2] explain SSIM as a generalized mean of 3-types of distortion criteria: changes in luminance, contrast, and structure. However, in the final formula in [1,2], some factors cancel out, producing a somewhat mysterious fraction

$$\frac{2\sigma_{xy}}{\sigma_x^2 + \sigma_y^2}$$

which no longer represents a proper measure of correlation (structure) or change in contrast.

Adding to the mystery, several suggestions have been made over the years that there must be some simple relation between SSIM and other distortion metrics, such as PSNR or MSE [7,8]. For instance, in 2010, A. Horé and D. Ziou [8] suggested that:

$$\frac{1-SSIM}{SSIM} \sim \frac{MSE}{2\sigma_{xy}},$$

where MSE is a mean square error and  $\sigma_{xy}$  is a covariance between image patches x and y. However, since  $\sigma_{xy}$  depends on both images, this formula does not reduce SSIM (as a distance metric between x and y) to MSE!

In this paper, we will look at SSIM again and offer an alternative model for its computation, leading to a more straightforward interpretation of the SSIM metric and its connection to MSE, SNR, and some other metrics. In Section 2, we will bring definitions, introduce our main results, and discuss their consequences. In Section 3, we will perform experimental validation of our proposed model for computing SSIM. In Section 4, we will drive conclusions.

# 2. Main Results and Their Consequences

## SSIM Definition

Recall that at a patch level, the SSIM between images x and y is defined as follows [1]:

$$SSIM(x,y) = \frac{2\mu_x\mu_y + C1}{\mu_x^2 + \mu_y^2 + C1} \cdot \frac{2\sigma_{xy} + C2}{\sigma_x^2 + \sigma_y^2 + C2}$$
(1)

where  $\mu_x, \mu_y, \sigma_x, \sigma_y, \sigma_{xy}$  represent patch-level statistics:

$$\mu_{x} = E[x] = \sum_{k=1}^{N} w_{k} x_{k}, \qquad (2)$$

$$\sigma_x^2 = \mathbf{E}[(x - \mu_x)^2] = \sum_{\substack{k=1 \ N}}^N w_k (x_k - \mu_x)^2,$$
(3)

$$\sigma_{xy} = \mathbf{E}[(x - \mu_x)(y - \mu_y)] = \sum_{k=1}^{\infty} w_k (x_k - \mu_x)(y_k - \mu_y), \tag{4}$$

and  $C_1, C_2$  are some small constants.

In the above formulae, operators E[.] denotes expectation with some density w superimposed over the patch. The original SSIM implementation [1] uses 11x11-pixel patches and circularsymmetric Gaussian density with a standard deviation  $\sigma = 1.5$ . The weights  $w_k$  are normalized:  $\sum_i w_i = 1$ .

The constants  $C_1$ ,  $C_2$  in the original SSIM design [1] are set to  $C_1 = (0.01 \cdot I_{\text{max}})^2$ , and  $C_2 = (0.03 \cdot I_{\text{max}})^2$ , where  $I_{max}$  is the maximum pixel value (e.g., 255 for 8-bit pixels). As explained in [1], the purpose of these constants is to avoid numerical instabilities when signals approach 0.

Considering the whole images, the mean SSIM is computed as the average of patch-level SSIMs at each pixel location (i, j):

$$\overline{SSIM}(x,y) = \frac{1}{WH} \sum_{i=1}^{W} \sum_{j=1}^{H} SSIM(x(i,j), y(i,j)).$$
(5)

W and H denote image width and height, respectively.

#### **Proposed Alternative Form**

By looking at formula (1), we first notice that SSIM is essentially a product of two nearly identical functions:

$$\xi(x,y) = \frac{2E[xy] + C}{E[x^2] + E[y^2] + C}$$
(6)

applied to different signals and at different scales. In the first term in the SSIM expression (1), this operation is applied to DC values  $\mu_x, \mu_y$ , treated as scalars (N = 1). In the second term in (1), this operation is applied to residual signals  $x - \mu_x$ , and  $y - \mu_y$ , observed in 11x11 patches ( $N = 11^2$ ).

However, if we examine the derivation of DC values  $\mu_x$ ,  $\mu_y$  in (1,2), we notice that they can also be understood as pixel values taken from some low-pass-filtered versions of input images  $x_L$ ,  $y_L$ . Similarly, we also realize that the residual signals in each path  $x - \mu_x$ , and  $y - \mu_y$  must be similar to signals taken from high-pass



Figure 1. Computation of SSIM by using formulae (7). SSIM is presented as a product of two identical distance measures  $\xi(.,.)$  computed for low-pass and high-pass filtered versions of input signals x, y.

versions of the same images:  $x_H = x - x_L$ ,  $y_H = y - y_L$ . And finally, we also notice that since DC values are coming from low-pass filtered images  $x_L$ ,  $y_L$ , then the relative distance between them as scalars  $\xi(\mu_x, \mu_y)$  or computed over surrounding patches  $\xi(x_L, y_L)$  must be very small. The low pass removes local variations making the patch-average results almost identical.

In other words, by combining all these observations, we can conjecture that patch-level SSIM can be computed in *a fully symmetric manner*, as follows

$$SSIM(x, y) \approx \xi(x_L, y_L) \cdot \xi(x_H, y_H) \tag{7}$$

where  $x_L$ ,  $y_L$  are the patches in low-pass filtered images,  $x_H = x - x_L$ ,  $y_H = y - y_L$  are the patches in high-pass filtered images, and where  $\xi(.,.)$  are identical distance functions (6) computed over patches in low-pass and high-pass images.

Figure 1 shows the flow-diagram explaining computations according to (7). In Section III, we present an experimental study, indicating that this process yields very similar results to the original SSIM formula. Our experiments further show that to split x, y into low-frequency and high-frequency components, it is sufficient to apply a Gaussian filter with pixel-level standard deviation  $\sigma = 3$ . This value is 2x larger than the standard deviation used in windows for computing patch-level distances  $\xi(x_L, y_L)$ ,  $\xi(x_H, y_H)$ .

#### Illustration of Operation

One of the immediate benefits of the proposed model (7) is a simple signal processing interpretation of how SSIM works and why it is better than full-band metrics, such as MSE or PSNR. We illustrate this in Figure 3.

As input x in this example, we use image k04 from the Kodak data set [17]. The low-pass  $(x_L)$  and high-pass  $(x_H)$  versions of this image are shown in the top row in Figure 2. The input y in this example is a reconstruction of the same image after it was compressed with H.264 encoder [18] with QP=47. This image is highly distorted relative to the original. The low-pass  $(y_L)$  and high-pass  $(y_H)$  versions of this image are shown in the middle row. Finally, the last row shows the differences between these images.

Looking at the last row, we immediately notice that the direct difference between input images x - y looks much "busier" compared to the difference images in low- and high-frequency domains. We see that the magnitudes of errors in each subband domain become lower (particularly in the low band), and their impacts become more obvious visually and conceptually. The low-pass filtering captures image changes in overall shapes, while high-pass shows differences in fine-grain details – contours, textures, etc.

In other words, we can see that the principal difference between SSIM and PSNR, MSE, and other simple metrics is that SSIM analyzes images in two subbands. Subband processing allows the



Figure. 2. Superimposed plots of Contrast Sensitivity Function CSF (black) and low- and high-pass filter responses (red and blue) in our SSIM model. Display Nyquist is assumed to be 40 cpd.

separation of errors such that their impacts can be more accurately measured and incorporated in the final score.

#### Connection to CSF

Let us next look at the split between bands used in our model for computing SSIM. The pixel-level standard deviation of the Gaussian low-pass filter used to produce  $x_L$  and  $y_L$  is  $\sigma = 3$ . Consequently, the cut-off frequency of this filter is  $f_c = \frac{F_s}{2\pi\sigma} \approx \frac{F_s}{18.85}$ , where  $F_s$  is the sampling rate. By assuming that display Nyquist frequency approximately matches the human visual acuity limit (which is typically the case for ITU-R BT-500 [20] visual tests), this implies that  $F_s$  must be about 80 cpd (cycles per degree), and therefore  $f_c \approx 4.244$  cpd.

As shown in Figure 2, this frequency approximately matches the peak of the Contrast Sensitivity Function (CSF) of human vision. This figure uses the Barten CSF model [19] and frequency responses of Gaussian low-pass and high-pass filters employed in our model for computing SSIM. Barten CSF model rendered for an observation angle  $X_0 = 30^\circ$  and object luminance L = 200 cd/m<sup>2</sup>.

This observation brings another argument suggesting why SSIM may be effective. It does a proper signal separation considering the involved mechanisms of human vision. Recall that the decay in contrast sensitivity in low- and high-frequency bands are caused by significantly different phenomena. In the high-band, sensitivity decay is mainly caused by the eye optical MTF [22]. In the low band, it is primarily the result of lateral inhibition [22,23]. The latter is a non-linear effect. The processing of low-band and high-band signals in the visual cortex is also different, as they turn into different sets of spatial frequency channels [23].

Even though in their motivations in [1], the authors of SSIM intended to design a metric that is not explicitly driven by the CSF and related phenomena of human vision, the use of patches and particular filters in the computation of SSIM, as we have shown above, leads back to this connection!

# Impacts of the Differences in Low- and Hight-Frequency Bands

By denoting each factor in SSIM expression (7) as  $\xi_L = \xi(x_L, y_L)$ , and  $\xi_H = \xi(x_H, y_H)$ , we can rewrite it as:

$$SSIM(\xi_L,\xi_H) = \xi_L \cdot \xi_H,$$

By using inequality between geometric and  $-\infty$  means, and also noting that  $\xi_L, \xi_H \leq 1$ , we can show that:

$$\operatorname{nin}(\xi_L,\xi_H)^2 \le SSIM(\xi_L,\xi_H) \le \operatorname{min}(\xi_L,\xi_H) \tag{8}$$

This inequality means that it is the smallest between subband differences  $\xi_L$  and  $\xi_H$  that has a limiting impact on the overall SSIM score!



 $x_L - y_L$ 

 $x_H - y_H$ 

Figure. 2. Visual illustration of steps in the proposed model for computation of SSIM. The top row shows an input image x and its low-pass  $x_L$  and high-pass  $x_H$  =  $x - x_L$  versions. The middle row shows the second input image y, and its low-pass  $y_L$  and high-pass  $y_H = y - y_L$  versions. This image is an encoded and decoded version of x, with significant distortions introduced by the codec. The bottom row shows the differences between the original images, as well as their filtered versions. It can be observed that full difference is much "busier" and less descriptive than low- and high-pass differences. Low-pass emphasizes changes in overall shapes, while high-pass emphasizes changes in textures, contours, and other fine features.

Consequently, this also means, is that if one tries to balance codec-introduced errors to maximize the overall SSIM value, then the best such balance would be achieved when the magnitudes of such errors in both bands are the same:

$$\max_{\delta: \xi_L = \xi_0 + \delta, \xi_H = \xi_0 - \delta} SSIM(\xi_L, \xi_H) \Rightarrow \xi_L = \xi_H.$$
(9)

This observation offers a simple principle for encoder optimizations improving SSIM scores. This idea may also lead to the design of a pre-processing filter that removes some of the lowfrequency features and thus allows the encoder to encode the remaining high-frequency content with fewer errors. With proper tuning, such a filter may enable existing encoders to achieve improved SSIM scores.

#### **Connection Between SSIM and Other Metrics**

Finally, let us now take a closer look at quantities  $\xi(x, y)$  in formula (7). For conceptual simplicity, we will discard constant C and will look instead at pure ratios:

$$\xi(x, y) = \frac{2E[xy]}{E[x^2] + E[y^2]}$$
(10)

We first note that ratio  $\xi(x, y)$  is not a proper measure of correlation. To measure correlation, one has to apply normalization by the geometric mean of  $E[x^2]$  and  $E[y^2]$ :

$$p(x,y) = \frac{E[xy]}{\sqrt{E[x^2]E[y^2]}}.$$
(11)

However, these quantities are related. By inequality between geometric and arithmetic means, we can see that:

$$\xi(x,y) \le \rho(x,y). \tag{12}$$

Next, by looking at the reciprocal of (9), we observe that:

$$\frac{1}{\xi(x,y)} = \frac{E[x^2] + E[(x+(y-x))^2]}{2E[xy]} = 1 + \frac{E[(y-x)^2]}{2E[xy]}$$

or, equivalently:

$$\frac{1-\xi(x,y)}{\xi(x,y)} = \frac{MSE(x,y)}{2E[xy]}$$
(13)

where  $MSE(x, y) = E[(x - y)^2]$  is the Mean Square Error.

The obtained formula (11) is similar to the result of A. Horé and D. Ziou [8], with an essential distinction that (13) is defined for subband signals. Horé and Ziou have assumed that DC differences are negligible (or equivalently, that  $\xi_L = 1$ ), but this is not always the case in practice. Equation (13) establishes a more general and accurate relation.

However, as we have already noted, formula (13) does not reduce  $\xi(x, y)$  to MSE(x, y), since E[xy] is a joint statistic of both signals. To produce a more direct relation, we rewrite (10) as:

$$\xi(x, y) = 1 - \frac{E[(y - x)^2]}{E[x^2] + E[y^2]}$$

and then:

$$\frac{1}{1 - \xi(x, y)} = SNR(x, y) + SNR(y, x)$$
(14)

where  $SNR(x, y) = \frac{E[x^2]}{E[(x-y)^2]}$  is the Signal to Noise Ratio.

Combining (14) and (7), we produce:

$$SSIM(x, y) \sim \left(1 - \frac{1}{SNR(x_L, y_L) + SNR(y_L, x_L)}\right) \times \left(1 - \frac{1}{SNR(x_H, y_H) + SNR(y_H, x_H)}\right)$$
(15)

where  $SNR(x_L, y_L)$ ,  $SNR(y_L, x_L)$ ,  $SNR(x_H, y_H)$ ,  $SNR(y_H, x_H)$  are signal-to-noise ratios computed for patches in low-pass and high-pass-filtered images respectively.

The formula (15) shows that SSIM can be computed using a combination of SNR metrics between low- and high-pass-filtered images. These derivations confirm that connections between SSIM and other objective metrics exist, but they are not as simple as suggested earlier in [7,8].

### 3. Experimental Validation

In this section, we describe tests performed to validate the accuracy of the proposed method for the computation of SSIM.

#### Methodology

For our experiments, we used 24 standard images from the Kodak dataset [17]. We have converted them to BT.709 YUV format and introduced three different types of distortions: 1) lossy compression artifacts, 2) Gaussian blur filtering, and 3) "salt-and-pepper" type noise.

In all cases, the SSIM values between the original and distorted images have been computed by method in the original paper [1]. Similarly, for all cases we have also computed SSIM values by the proposed method (7). For band separation, we used a circular-symmetric Gaussian filter with  $\sigma = 3$ . The differences between SSIM values obtained by our method and the reference method [1] are reported in Tables I-IV.

To measure the degree of mismatch between our proposed method and the original one [1] we have reported the differences (Deltas) in SSIM values for all files and compound RMS differences across the entire set. If such differences are negligibly small, this implies that the proposed process is as effective for predicting of MOS scores as the original SSIM metric [1].

#### Accuracy Tests using Compression Artifacts

Tables 2 and 2 report the accuracy of our method in the cases of lossy compression artifacts. Such artifacts have been introduced by using the H.264 video encoder [18], operating in Main Profile, "slow" encoding preset, and using fixed-QP rate control mode. QP values of 17, 22, 27, 32, 37, 42, and 47 have been used to control the degree of artifacts introduced. The columns "SSIM" list the reference SSIM values [1], and the column "Delta" lists the differences between the reference SSIM and the one calculated by our method. Y-channel frame-average SSIM values are used as the basis for comparison. The last rows list RMS average values across all files.

Table 2 reports results for 1536x1024 resolution compressed images, and Table 2 reports results for 384x256 resolution images. It can be observed that the differences between SSIM values computed by using our model and reference are very small, despite the broad range of variation of SSIM values, distortion, resolutions, and content types.

#### Accuracy Tests using Gaussian Blur

Table 3 reports the accuracy of our method in cases of blur artifacts. Such artifacts have been introduced by applying a circular-symmetric Gaussian blur filter, with variance parameter  $\sigma$  set to values 0.5, 0.7, 1, 3, 5, 10, and 15. As can be observed, our method shows reasonably accurate performance in all these tests. The most significant deviations are observed for blur value  $\sigma = 5$ , when SSIM values are at around 0.4...0.7. However, the errors clearly vanish with smaller or larger values of  $\sigma$  (low and high-blur regimes).

|      |        |         |        |         | -      |         |        |         |        |         |        |         | -      |         |
|------|--------|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|---------|
| File | QP     | 9=17    | QP     | 9=22    | QF     | 9=27    | QP     | =32     | QP=37  |         | QP=42  |         | QF     | 9=47    |
|      | SSIM   | Delta   |
| k01  | 0.9949 | 0.0003  | 0.9867 | 0.0008  | 0.9697 | 0.0016  | 0.9337 | 0.0028  | 0.8687 | 0.0038  | 0.7766 | 0.0026  | 0.6648 | -0.0026 |
| k02  | 0.9928 | 0.0000  | 0.9784 | 0.0001  | 0.9447 | 0.0001  | 0.8962 | -0.0009 | 0.8318 | -0.0033 | 0.7569 | -0.0069 | 0.6843 | -0.0119 |
| k03  | 0.9879 | 0.0000  | 0.9768 | -0.0001 | 0.9669 | -0.0003 | 0.9506 | -0.0008 | 0.9251 | -0.0016 | 0.8947 | -0.0033 | 0.8617 | -0.0059 |
| k05  | 0.9906 | -0.0001 | 0.9782 | -0.0004 | 0.9603 | -0.0009 | 0.9327 | -0.0018 | 0.8937 | -0.0034 | 0.8453 | -0.0063 | 0.7928 | -0.0108 |
| k06  | 0.9941 | 0.0003  | 0.9869 | 0.0005  | 0.9757 | 0.0007  | 0.9551 | 0.0008  | 0.9168 | 0.0004  | 0.8552 | -0.0015 | 0.7619 | -0.0067 |
| k07  | 0.9930 | 0.0001  | 0.9851 | 0.0003  | 0.9709 | 0.0006  | 0.9427 | 0.0006  | 0.8920 | 0.0000  | 0.8126 | -0.0027 | 0.7108 | -0.0076 |
| k08  | 0.9889 | -0.0002 | 0.9781 | -0.0004 | 0.9707 | -0.0008 | 0.9599 | -0.0016 | 0.9427 | -0.0030 | 0.9173 | -0.0056 | 0.8811 | -0.0087 |
| k11  | 0.9956 | 0.0003  | 0.9853 | 0.0010  | 0.9626 | 0.0022  | 0.9326 | 0.0030  | 0.8876 | 0.0030  | 0.8180 | 0.0019  | 0.7076 | -0.0030 |
| k12  | 0.9893 | 0.0000  | 0.9623 | 0.0001  | 0.9320 | -0.0001 | 0.9180 | -0.0006 | 0.8989 | -0.0016 | 0.8708 | -0.0038 | 0.8376 | -0.0065 |
| k13  | 0.9898 | 0.0000  | 0.9645 | 0.0001  | 0.9328 | -0.0004 | 0.9149 | -0.0014 | 0.8931 | -0.0031 | 0.8649 | -0.0055 | 0.8321 | -0.0084 |
| k14  | 0.9918 | 0.0002  | 0.9799 | 0.0004  | 0.9611 | 0.0006  | 0.9264 | 0.0004  | 0.8701 | -0.0012 | 0.8019 | -0.0044 | 0.7361 | -0.0083 |
| k15  | 0.9887 | 0.0000  | 0.9776 | -0.0002 | 0.9646 | -0.0005 | 0.9443 | -0.0015 | 0.9169 | -0.0029 | 0.8888 | -0.0049 | 0.8673 | -0.0063 |
| k16  | 0.9967 | 0.0001  | 0.9911 | 0.0003  | 0.9753 | 0.0006  | 0.9363 | 0.0011  | 0.8557 | 0.0005  | 0.7283 | -0.0034 | 0.5750 | -0.0123 |
| k20  | 0.9932 | 0.0001  | 0.9826 | 0.0001  | 0.9637 | -0.0001 | 0.9281 | -0.0014 | 0.8704 | -0.0046 | 0.7942 | -0.0102 | 0.7149 | -0.0162 |
| k21  | 0.9909 | -0.0001 | 0.9805 | -0.0003 | 0.9645 | -0.0007 | 0.9393 | -0.0017 | 0.9069 | -0.0033 | 0.8707 | -0.0050 | 0.8339 | -0.0073 |
| k22  | 0.9907 | 0.0000  | 0.9804 | 0.0000  | 0.9677 | -0.0001 | 0.9433 | -0.0003 | 0.8989 | -0.0009 | 0.8316 | -0.0029 | 0.7461 | -0.0078 |
| k23  | 0.9908 | -0.0002 | 0.9687 | -0.0007 | 0.9367 | -0.0018 | 0.9121 | -0.0035 | 0.8840 | -0.0055 | 0.8510 | -0.0079 | 0.8090 | -0.0101 |
| k24  | 0.9945 | 0.0000  | 0.9820 | -0.0001 | 0.9431 | -0.0004 | 0.8858 | -0.0015 | 0.8310 | -0.0038 | 0.7617 | -0.0077 | 0.6729 | -0.0136 |
| k04  | 0.9913 | 0.0001  | 0.9741 | 0.0000  | 0.9555 | 0.0000  | 0.9282 | 0.0002  | 0.8788 | -0.0003 | 0.8172 | -0.0023 | 0.7594 | -0.0041 |
| k09  | 0.9889 | 0.0000  | 0.9739 | -0.0001 | 0.9632 | -0.0001 | 0.9453 | -0.0003 | 0.9128 | -0.0011 | 0.8726 | -0.0033 | 0.8375 | -0.0052 |
| k10  | 0.9912 | 0.0000  | 0.9701 | 0.0001  | 0.9484 | 0.0001  | 0.9269 | 0.0001  | 0.8918 | -0.0003 | 0.8395 | -0.0024 | 0.7723 | -0.0082 |
| k17  | 0.9913 | -0.0001 | 0.9765 | -0.0002 | 0.9562 | -0.0006 | 0.9225 | -0.0017 | 0.8716 | -0.0040 | 0.8097 | -0.0076 | 0.7471 | -0.0108 |
| k18  | 0.9877 | -0.0004 | 0.9705 | -0.0010 | 0.9575 | -0.0017 | 0.9441 | -0.0026 | 0.9286 | -0.0037 | 0.9107 | -0.0046 | 0.8900 | -0.0048 |
| k19  | 0.9928 | 0.0002  | 0.9846 | 0.0003  | 0.9718 | 0.0002  | 0.9471 | -0.0004 | 0.9041 | -0.0024 | 0.8395 | -0.0069 | 0.7560 | -0.0139 |
| RMS  | 0.9915 | 0.0002  | 0.9781 | 0.0004  | 0.9591 | 0.0009  | 0.9321 | 0.0016  | 0.8909 | 0.0028  | 0.8360 | 0.0052  | 0.7727 | 0.0091  |
|      |        |         |        |         |        |         |        |         |        |         |        |         |        |         |

Table 1: Accuracy of the proposed method for computing SSIM: H.264 Encoding/Decoding tests, 1536x1024-resolution images.

Table 2: Accuracy of the proposed method for computing SSIM: H.264 Encoding/Decoding tests, 384x256-resolution images.

| File | QP=17  |         | QP=22  |         | QF     | =27     | QP     | =32     | QP=37  |         | QP=42  |         | QP=47  |         |
|------|--------|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|---------|--------|---------|
|      | SSIM   | Delta   |
| k01  | 0.9969 | 0.0003  | 0.9919 | 0.0009  | 0.9778 | 0.0024  | 0.9432 | 0.0051  | 0.8677 | 0.0080  | 0.7410 | 0.0088  | 0.5773 | 0.0027  |
| k02  | 0.9950 | 0.0001  | 0.9853 | 0.0002  | 0.9517 | 0.0007  | 0.8700 | 0.0015  | 0.7556 | 0.0009  | 0.6430 | -0.0030 | 0.5636 | -0.0070 |
| k03  | 0.9918 | 0.0002  | 0.9824 | 0.0005  | 0.9654 | 0.0011  | 0.9366 | 0.0020  | 0.8949 | 0.0028  | 0.8402 | 0.0015  | 0.7862 | -0.0028 |
| k05  | 0.9980 | 0.0001  | 0.9944 | 0.0004  | 0.9836 | 0.0011  | 0.9547 | 0.0026  | 0.8912 | 0.0051  | 0.7740 | 0.0076  | 0.6151 | 0.0059  |
| k06  | 0.9953 | 0.0001  | 0.9886 | 0.0003  | 0.9697 | 0.0008  | 0.9247 | 0.0016  | 0.8412 | 0.0024  | 0.7186 | 0.0008  | 0.6121 | 0.0001  |
| k07  | 0.9945 | 0.0003  | 0.9901 | 0.0006  | 0.9807 | 0.0010  | 0.9608 | 0.0015  | 0.9225 | 0.0014  | 0.8503 | -0.0008 | 0.7445 | -0.0055 |
| k08  | 0.9973 | 0.0003  | 0.9926 | 0.0009  | 0.9813 | 0.0017  | 0.9557 | 0.0029  | 0.9108 | 0.0042  | 0.8313 | 0.0052  | 0.6982 | 0.0066  |
| k11  | 0.9948 | 0.0002  | 0.9865 | 0.0006  | 0.9653 | 0.0012  | 0.9178 | 0.0021  | 0.8447 | 0.0014  | 0.7619 | -0.0003 | 0.6688 | -0.0050 |
| k12  | 0.9911 | 0.0002  | 0.9786 | 0.0004  | 0.9568 | 0.0008  | 0.9233 | 0.0011  | 0.8905 | 0.0011  | 0.8573 | 0.0009  | 0.8137 | -0.0018 |
| k13  | 0.9980 | 0.0001  | 0.9944 | 0.0001  | 0.9813 | 0.0005  | 0.9392 | 0.0012  | 0.8402 | 0.0015  | 0.6761 | -0.0018 | 0.4950 | -0.0077 |
| k14  | 0.9966 | 0.0001  | 0.9899 | 0.0002  | 0.9710 | 0.0007  | 0.9242 | 0.0013  | 0.8355 | 0.0004  | 0.7192 | -0.0035 | 0.5829 | -0.0122 |
| k15  | 0.9927 | 0.0001  | 0.9840 | 0.0002  | 0.9689 | 0.0006  | 0.9408 | 0.0014  | 0.9037 | 0.0018  | 0.8583 | 0.0010  | 0.8070 | -0.0004 |
| k16  | 0.9933 | -0.0001 | 0.9841 | -0.0000 | 0.9628 | -0.0001 | 0.9173 | -0.0004 | 0.8406 | -0.0013 | 0.7478 | -0.0033 | 0.6594 | -0.0089 |
| k20  | 0.9926 | 0.0001  | 0.9886 | 0.0002  | 0.9792 | 0.0003  | 0.9542 | 0.0004  | 0.9050 | -0.0002 | 0.8587 | -0.0013 | 0.8115 | -0.0023 |
| k21  | 0.9926 | 0.0001  | 0.9869 | 0.0002  | 0.9771 | 0.0005  | 0.9557 | 0.0010  | 0.9138 | 0.0018  | 0.8409 | 0.0016  | 0.7431 | -0.0020 |
| k22  | 0.9941 | 0.0001  | 0.9857 | 0.0001  | 0.9645 | 0.0002  | 0.9137 | -0.0001 | 0.8236 | -0.0022 | 0.7170 | -0.0077 | 0.6206 | -0.0146 |
| k23  | 0.9912 | -0.0005 | 0.9842 | -0.0009 | 0.9712 | -0.0016 | 0.9455 | -0.0029 | 0.9075 | -0.0049 | 0.8627 | -0.0077 | 0.8103 | -0.0094 |
| k24  | 0.9962 | 0.0002  | 0.9902 | 0.0005  | 0.9748 | 0.0011  | 0.9379 | 0.0019  | 0.8555 | 0.0021  | 0.7358 | -0.0003 | 0.5889 | -0.0131 |
| k04  | 0.9932 | -0.0001 | 0.9842 | -0.0004 | 0.9657 | -0.0009 | 0.9286 | -0.0017 | 0.8666 | -0.0029 | 0.7817 | -0.0057 | 0.6949 | -0.0093 |
| k09  | 0.9909 | 0.0002  | 0.9861 | 0.0004  | 0.9781 | 0.0007  | 0.9618 | 0.0012  | 0.9269 | 0.0013  | 0.8671 | 0.0014  | 0.7850 | -0.0018 |
| k10  | 0.9919 | 0.0001  | 0.9836 | 0.0001  | 0.9689 | 0.0001  | 0.9413 | -0.0002 | 0.8947 | -0.0006 | 0.8198 | -0.0031 | 0.7291 | -0.0076 |
| k17  | 0.9942 | 0.0001  | 0.9844 | 0.0003  | 0.9667 | 0.0003  | 0.9323 | 0.0002  | 0.8739 | -0.0014 | 0.7943 | -0.0046 | 0.6908 | -0.0113 |
| k18  | 0.9958 | 0.0001  | 0.9883 | 0.0003  | 0.9729 | 0.0007  | 0.9371 | 0.0012  | 0.8556 | 0.0012  | 0.7069 | -0.0022 | 0.5463 | -0.0103 |
| k19  | 0.9931 | -0.0001 | 0.9835 | -0.0001 | 0.9655 | -0.0004 | 0.9224 | -0.0007 | 0.8412 | -0.0025 | 0.7715 | -0.0039 | 0.7010 | -0.0033 |
| RMS  | 0.9942 | 0.0002  | 0.9871 | 0.0004  | 0.9709 | 0.0010  | 0.9352 | 0.0018  | 0.8718 | 0.0028  | 0.7850 | 0.0041  | 0.6874 | 0.0075  |

## Accuracy Tests using Salt-and-Pepper Noise

Finally, Table 4 reports the accuracy of our method in the cases of "salt and pepper" noise. This noise was introduced by negating a random subset of pixel values in the image. A binary random noise generator with pixel-level flip probabilities of p = 0.0001, 0.0005, 0.001, 0.005, 0.01, 0.05, and 0.1 have been utilized. The same method was applied to all files. As can be observed, our method achieves high accuracy in computing SSIM values in all these tests.

| File | sigma=0.5 |         | sigma=0.7 |         | sigma=1 |         | sigi   | ma=3    | sigma=5 |         | sigma=10 |         | sigma=15 |         |
|------|-----------|---------|-----------|---------|---------|---------|--------|---------|---------|---------|----------|---------|----------|---------|
|      | SSIM      | Delta   | SSIM      | Delta   | SSIM    | Delta   | SSIM   | Delta   | SSIM    | Delta   | SSIM     | Delta   | SSIM     | Delta   |
| k01  | 0.9872    | 0.0005  | 0.9468    | 0.0016  | 0.8731  | 0.0021  | 0.5532 | -0.0172 | 0.4774  | -0.0322 | 0.4412   | -0.0279 | 0.4359   | -0.0255 |
| k02  | 0.9857    | 0.0001  | 0.9471    | 0.0001  | 0.8893  | -0.0009 | 0.6828 | -0.0182 | 0.6428  | -0.0176 | 0.6224   | -0.0138 | 0.6187   | -0.0115 |
| k03  | 0.9940    | 0.0000  | 0.9798    | -0.0000 | 0.9590  | -0.0005 | 0.8661 | -0.0130 | 0.8385  | -0.0144 | 0.8206   | -0.0116 | 0.8168   | -0.0098 |
| k05  | 0.9939    | 0.0001  | 0.9758    | 0.0002  | 0.9381  | -0.0007 | 0.6611 | -0.0263 | 0.5565  | -0.0367 | 0.4901   | -0.0281 | 0.4790   | -0.0237 |
| k06  | 0.9900    | 0.0002  | 0.9589    | 0.0006  | 0.9034  | 0.0002  | 0.6571 | -0.0160 | 0.6000  | -0.0216 | 0.5724   | -0.0180 | 0.5685   | -0.0161 |
| k07  | 0.9949    | -0.0001 | 0.9836    | -0.0004 | 0.9678  | -0.0014 | 0.8729 | -0.0166 | 0.8066  | -0.0140 | 0.7474   | -0.0071 | 0.7393   | -0.0032 |
| k08  | 0.9845    | 0.0005  | 0.9380    | 0.0014  | 0.8623  | 0.0008  | 0.5444 | -0.0226 | 0.4592  | -0.0416 | 0.4062   | -0.0338 | 0.3968   | -0.0291 |
| k11  | 0.9895    | 0.0001  | 0.9593    | 0.0003  | 0.9090  | -0.0005 | 0.7008 | -0.0191 | 0.6498  | -0.0234 | 0.6199   | -0.0188 | 0.6138   | -0.0163 |
| k12  | 0.9944    | 0.00001 | 0.9803    | -0.0001 | 0.9587  | -0.0009 | 0.8678 | -0.0140 | 0.8430  | -0.0156 | 0.8281   | -0.0135 | 0.8254   | -0.0122 |
| k13  | 0.9814    | 0.0003  | 0.9239    | 0.0008  | 0.8271  | -0.0002 | 0.4635 | -0.0177 | 0.3853  | -0.0260 | 0.3453   | -0.0196 | 0.3390   | -0.0161 |
| k14  | 0.9908    | -0.0000 | 0.9648    | -0.0003 | 0.9196  | -0.0021 | 0.6939 | -0.0267 | 0.6232  | -0.0297 | 0.5778   | -0.0221 | 0.5690   | -0.0175 |
| k15  | 0.9926    | -0.0000 | 0.9724    | -0.0003 | 0.9419  | -0.0013 | 0.8280 | -0.0141 | 0.7954  | -0.0163 | 0.7696   | -0.0118 | 0.7628   | -0.0089 |
| k16  | 0.9900    | 0.0001  | 0.9606    | 0.0004  | 0.9124  | -0.0001 | 0.7310 | -0.0143 | 0.6928  | -0.0157 | 0.6740   | -0.0129 | 0.6708   | -0.0112 |
| k20  | 0.9916    | 0.0000  | 0.9700    | -0.0000 | 0.9385  | -0.0006 | 0.8238 | -0.0111 | 0.7926  | -0.0142 | 0.7708   | -0.0108 | 0.7663   | -0.0090 |
| k21  | 0.9878    | 0.0001  | 0.9557    | 0.0001  | 0.9082  | -0.0011 | 0.7223 | -0.0158 | 0.6712  | -0.0218 | 0.6405   | -0.0170 | 0.6351   | -0.0142 |
| k22  | 0.9904    | 0.0000  | 0.9644    | -0.0001 | 0.9232  | -0.0010 | 0.7471 | -0.0190 | 0.6970  | -0.0167 | 0.6693   | -0.0115 | 0.6645   | -0.0084 |
| k23  | 0.9939    | -0.0001 | 0.9807    | -0.0006 | 0.9640  | -0.0014 | 0.8961 | -0.0109 | 0.8708  | -0.0096 | 0.8530   | -0.0061 | 0.8490   | -0.0036 |
| k24  | 0.9928    | 0.0000  | 0.9716    | -0.0003 | 0.9313  | -0.0019 | 0.7097 | -0.0257 | 0.6430  | -0.0291 | 0.6043   | -0.0230 | 0.5975   | -0.0193 |
| k04  | 0.9914    | -0.0001 | 0.9687    | -0.0004 | 0.9337  | -0.0016 | 0.7888 | -0.0177 | 0.7475  | -0.0197 | 0.7197   | -0.0149 | 0.7136   | -0.0116 |
| k09  | 0.9883    | 0.0001  | 0.9619    | 0.0001  | 0.9309  | -0.0006 | 0.8252 | -0.0134 | 0.7875  | -0.0168 | 0.7638   | -0.0133 | 0.7600   | -0.0112 |
| k10  | 0.9890    | 0.00002 | 0.9643    | -0.0001 | 0.9348  | -0.0011 | 0.8257 | -0.0174 | 0.7868  | -0.0190 | 0.7603   | -0.0149 | 0.7554   | -0.0123 |
| k17  | 0.9882    | -0.0002 | 0.9606    | -0.0009 | 0.9265  | -0.0026 | 0.8062 | -0.0190 | 0.7605  | -0.0187 | 0.7210   | -0.0113 | 0.7112   | -0.0062 |
| k18  | 0.9825    | 0.0000  | 0.9366    | -0.0001 | 0.8736  | -0.0016 | 0.6315 | -0.0202 | 0.5542  | -0.0193 | 0.5074   | -0.0112 | 0.4998   | -0.0068 |
| k19  | 0.9887    | 0.0001  | 0.9576    | 0.0002  | 0.9083  | -0.0004 | 0.7159 | -0.0137 | 0.6660  | -0.0202 | 0.6396   | -0.0169 | 0.6352   | -0.0150 |
| RMS  | 0.9897    | 0.0002  | 0.9619    | 0.0006  | 0.9187  | 0.0012  | 0.7422 | 0.0180  | 0.6928  | 0.0226  | 0.6623   | 0.0175  | 0.6567   | 0.0147  |

Table 3: Accuracy of the proposed method for computing SSIM: Gaussian blur tests, 1536x1024-resolution images.

Table 4: Accuracy of the proposed method for computing SSIM: Salt-and-pepper noise tests, 1536x1024-resolution images.

| File | p=0.00001 |          | p=0.0005 |          | p=0.001 |          | p=0.005 |          | p=0.01 |          | p=0.05 |          | p=0.1  |          |
|------|-----------|----------|----------|----------|---------|----------|---------|----------|--------|----------|--------|----------|--------|----------|
|      | SSIM      | Delta    | SSIM     | Delta    | SSIM    | Delta    | SSIM    | Delta    | SSIM   | Delta    | SSIM   | Delta    | SSIM   | Delta    |
| k01  | 0.9990    | 0.00001  | 0.9942   | 0.00016  | 0.9885  | 0.00039  | 0.9468  | 0.00179  | 0.9006 | 0.00308  | 0.6630 | 0.00715  | 0.5142 | 0.00692  |
| k02  | 0.9976    | 0.00001  | 0.9870   | 0.00002  | 0.9741  | 0.00003  | 0.8768  | -0.00020 | 0.7745 | -0.00089 | 0.3532 | -0.00377 | 0.1961 | -0.00228 |
| k03  | 0.9983    | 0.00001  | 0.9911   | 0.00001  | 0.9827  | 0.00000  | 0.9188  | -0.00026 | 0.8509 | -0.00082 | 0.5485 | -0.00307 | 0.4078 | -0.00254 |
| k05  | 0.9984    | 0.00006  | 0.9911   | 0.00025  | 0.9825  | 0.00049  | 0.9192  | 0.00181  | 0.8509 | 0.00298  | 0.5387 | 0.00301  | 0.3819 | 0.00123  |
| k06  | 0.9982    | 0.00001  | 0.9911   | 0.00007  | 0.9825  | 0.00016  | 0.9179  | 0.00045  | 0.8491 | 0.00064  | 0.5518 | 0.00166  | 0.4094 | 0.00264  |
| k07  | 0.9986    | -0.00002 | 0.9934   | -0.00013 | 0.9866  | -0.00016 | 0.9371  | -0.00113 | 0.8816 | -0.00216 | 0.6063 | -0.00724 | 0.4528 | -0.00830 |
| k08  | 0.9989    | 0.00002  | 0.9932   | 0.00019  | 0.9863  | 0.00038  | 0.9363  | 0.00179  | 0.8835 | 0.00291  | 0.6264 | 0.00496  | 0.4778 | 0.00392  |
| k11  | 0.9986    | 0.00002  | 0.9931   | 0.00007  | 0.9864  | 0.00012  | 0.9382  | 0.00043  | 0.8871 | 0.00061  | 0.6625 | 0.00104  | 0.5411 | 0.00104  |
| k12  | 0.9975    | 0.00000  | 0.9866   | -0.00001 | 0.9734  | 0.00000  | 0.8750  | -0.00028 | 0.7710 | -0.00092 | 0.3464 | -0.00354 | 0.1932 | -0.00192 |
| k13  | 0.9989    | 0.00002  | 0.9948   | 0.00006  | 0.9899  | 0.00014  | 0.9502  | 0.00065  | 0.9051 | 0.00102  | 0.6692 | 0.00215  | 0.5182 | 0.00206  |
| k14  | 0.9983    | -0.00001 | 0.9919   | 0.00001  | 0.9836  | 0.00005  | 0.9203  | 0.00020  | 0.8522 | 0.00008  | 0.5449 | -0.00125 | 0.3951 | -0.00142 |
| k15  | 0.9969    | -0.00003 | 0.9830   | -0.00014 | 0.9664  | -0.00027 | 0.8471  | -0.00163 | 0.7254 | -0.00347 | 0.2905 | -0.00677 | 0.1656 | -0.00320 |
| k16  | 0.9986    | 0.00000  | 0.9930   | 0.00003  | 0.9860  | 0.00005  | 0.9334  | 0.00011  | 0.8776 | 0.00007  | 0.6103 | -0.00076 | 0.4690 | -0.00058 |
| k20  | 0.9968    | -0.00003 | 0.9823   | -0.00016 | 0.9651  | -0.00031 | 0.8439  | -0.00179 | 0.7217 | -0.00360 | 0.3071 | -0.00476 | 0.1912 | -0.00147 |
| k21  | 0.9988    | 0.00001  | 0.9938   | 0.00003  | 0.9873  | 0.00010  | 0.9406  | 0.00049  | 0.8876 | 0.00066  | 0.6170 | -0.00006 | 0.4562 | -0.00111 |
| k22  | 0.9986    | 0.00000  | 0.9927   | 0.00001  | 0.9859  | 0.00000  | 0.9326  | -0.00023 | 0.8746 | -0.00061 | 0.5899 | -0.00272 | 0.4396 | -0.00260 |
| k23  | 0.9981    | -0.00001 | 0.9897   | -0.00013 | 0.9800  | -0.00027 | 0.9056  | -0.00137 | 0.8247 | -0.00265 | 0.4756 | -0.00734 | 0.3257 | -0.00627 |
| k24  | 0.9984    | 0.00003  | 0.9919   | 0.00007  | 0.9844  | 0.00012  | 0.9287  | 0.00050  | 0.8680 | 0.00065  | 0.5866 | 0.00007  | 0.4381 | -0.00065 |
| k04  | 0.9983    | 0.00000  | 0.9907   | -0.00003 | 0.9814  | -0.00005 | 0.9151  | -0.00056 | 0.8437 | -0.00128 | 0.5239 | -0.00479 | 0.3757 | -0.00494 |
| k09  | 0.9985    | 0.00001  | 0.9922   | 0.00004  | 0.9843  | 0.00007  | 0.9262  | 0.00013  | 0.8637 | 0.00007  | 0.5616 | -0.00171 | 0.4066 | -0.00218 |
| k10  | 0.9987    | 0.00001  | 0.9938   | -0.00001 | 0.9879  | 0.00003  | 0.9427  | 0.00005  | 0.8930 | -0.00014 | 0.6488 | -0.00223 | 0.5126 | -0.00324 |
| k17  | 0.9974    | -0.00003 | 0.9875   | -0.00018 | 0.9756  | -0.00036 | 0.8880  | -0.00184 | 0.7981 | -0.00363 | 0.4439 | -0.00773 | 0.3067 | -0.00594 |
| k18  | 0.9981    | -0.00001 | 0.9902   | -0.00002 | 0.9799  | -0.00009 | 0.9048  | -0.00068 | 0.8238 | -0.00151 | 0.4680 | -0.00462 | 0.3091 | -0.00354 |
| k19  | 0.9988    | 0.00002  | 0.9938   | 0.00013  | 0.9874  | 0.00026  | 0.9408  | 0.00109  | 0.8888 | 0.00172  | 0.6252 | 0.00182  | 0.4751 | 0.00021  |
| RMS  | 0.9983    | 0.00002  | 0.9909   | 0.00011  | 0.9820  | 0.00022  | 0.9165  | 0.00103  | 0.8473 | 0.00193  | 0.5474 | 0.00423  | 0.4051 | 0.00360  |

# 4. Conclusions

In this paper, we have proposed an alternative model of SSIM computation, utilizing subband decomposition and identical distance

measures in each subband. We have shown that this model performs very close to the original under various visual content types, resolutions, and distortions introduced. Specifically, we have studied its performance with a broad range of lossy compression artifacts, Gaussian blur, and "salt-and-pepper"-type noise. We have also explained the benefits of the proposed model from practical and methodological perspectives. Such benefits include a simple and intuitive explanation of why SSIM works better than fullband metrics, its connection to CSF and related phenomena of vision, SSIM-boosting pre-filtering and encoder optimization techniques, and mathematical connections between SSIM, MSE, and SNR metrics.

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