# Texture re-rendering tool for re-mixing indoor scene images 

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#### Abstract

We propose a novel tool for re-rendering objects in indoor scene images with new textures. It aims to address the problem of too much manual work of positioning and alignment when applying new texture onto an object surface in an indoor scene image. The algorithm of the tool is based on establishing 2D projective transformation between texture images and planar object surfaces in scene images. In order to find the transformation, we use a sampled rectangular texture pattern from a large synthesized planar texture and a planar quadrangle corresponding to object surface orientation estimation, which is generated by a geometric orientation hypothesis framework. The tool also puts effort in adjusting the scaling and reducing artifacts for re-rendered textures. We present the re-rendering results for ceilings, walls, floors, etc. that naturally correspond to room geometry layout.


## 1. Introduction

Digital imaging and rendering technology has brought us tremendous amount of benefits, one of which is the privilege of creating variable media contents through user customizations. One case that is receiving increasing interest these days, is in the application of customizing images on websites. Specifically, users can replace some part of images that is already on websites with new textures that they prefer, and then create new images by mixing up the replaced texture with original images. This kind of customization is known as image personalization [1]. The specific instance of image personalization to which our tool is targeted is the virtual customization of images taken from indoor scenes of residential structures, such as kitchen, living room or bedroom. This kind of customization lets users replace the original textures from object surfaces in the scene with preferred new textures, which is called texture re-rendering and image re-mixing. Figure 1 shows examples of texture re-rendering and image re-mixing. In the figure, the original floor textures and/or side wall textures from the indoor bathroom image are replaced with new types of textures, and then a re-mixed scene image is created. Figure 1b and Figure 1 d separately show us that original appearance of floor and/or side wall is replaced by wooden and brick like textures. The highlighted green lines in Figure 1a illustrate the orientation of parallel lines within original floor texture. And the highlighted yellow lines in Figure 1 b illustrate the orientation of parallel lines within replaced wooden-like texture. The brick-like texture in Figure 1d is clearly showing the orientation of parallel lines. By comparing the parallel line orientations in the re-rendered texture in Figure 1 b and Figure 1d, we are able to see that the re-rendering result in Figure 1d looks more natural than that in Figure 1b, with respect to the room spatial layout. The position and orientation of the re-rendered texture in Figure 1b apparently needs to be manually adjusted before it appears to natrually corresponds to room spatial layout. Figure 1c shows a different type of texture replacement,


Figure 1. Examples of texture re-rendering for the indoor bathroom image. Highlighted lines show the orientation of parallel lines in floor texture. (a) Original scene image taken from bathroom (b) Re-rendered floor and side wall with wooden texture. (c) Re-rendered side-wall with pure color texture. (d) Re-rendered floor with brick texture that naturally corresponds to geometry layout of the room.
where the surface of side walls is replaced with pure color textures. This type of texture re-render, however, can only be suitable to the situation where original textures of the object surface have no complicated texture patterns. Currently, several commercial websites has been devoted to developing web-based interfaces for indoor scene image re-texturing, among which [6]-[9] are quite noticeable. [7] and [8] provide a functionality that is similar to the one shown in Figure 1c. [7] and [9] let users apply preferred textures in a virtual design environment. Although the visualization tool provides quite reasonable rendering result, it is hard to see the effect of newly applied texture in original scene images. As for [6], which provides a functionality as shown in Figure 1b, even though their tools are able to let users select various types of textures and render them in the original scene images, the result does not look as if it is naturally corresponding to the geometry orientation of the scene, thus an amount of manual adjustment afterwards is needed. In addition, the zoomed-in view of their rendered texture has poor quality. As a result, a tool is desired that has the following properties: firstly, it supports various types of textures; secondly, it is able to allow the re-rendered texture be directly mixed with the original scene image; thirdly, the rerendering result natrually corresponds to room layout; finally, it is able to allow high-resolution rendering. Our proposed tool aims at these targets. In [1], the authors proposed a method for inserting text in images based on pinhole camera model with camera
parameter estimation. However, text-insertion usually happens within a limited spatial range, thus the error for parameter estimation is not going to greatly affect the alignment and orientation of inserted text. In addition, their approach is based on straight line detection where the lines are either perpendicular or parallel with each other. This is not applicable to indoor scene images since straight lines in these images do not have to be aligned either horizontally or vertically to each other.

In this paper, we propose a texture re-rendering tool that is based on 2D projective geometry [3], and we are specially focused on establishing the 2 D projective transformation from texture images to scene images. To begin with, we adopt a room layout estimation framework proposed in [2], which is based on line sweeping algorithm and convex edge detection to generate layout hypothesis. And then we apply Direct Linear Transform (DLT) algorithm to calculate the transformation matrix for texture mapping. The details are discussed in the rest of the paper.

## 2. Projective Geometry

In this section, we briefly introduce projective geometry, which is the study of 2D planar geometry, as the starting point for our texture re-rendering method. And in the following discussions, we denote 2D plane as $\mathbb{P}^{2}$.

### 2.1 Homogeneous representation for 2D points

The coordinate pair $(x, y)$ can represent a point in 2D plane. Therefore we identify a plane as $\mathbb{R}^{2}$, and the coordinate pair $(x, y)$ is then identified as a 2 D vector, thus a plane can be considered as a vector space. A point $(x, y) \in \mathbb{R}^{2}$ lies on line $(a, b, c)$ if and only if $a x+b y+1=0$, which, in matrix form, can be written as $(x, y, 1) \cdot(a, b, c)^{\top}=1$. Here we can see that $(x, y) \in \mathbb{R}^{2}$ is represented as a 3D vector $(x, y, 1)$. And since it is also true that $k(x, y, z) \cdot(a, b, c)^{\top}=0$, we are able to draw the conclusion that ( $k x, k y, k$ ) and $(x, y, 1)$ represents the same point $(x, y)$ in $\mathbb{P}^{2}$, thus the 3 -vector representative of the form $\left(x_{1}, x_{2}, x_{3}\right)$, where $x_{3} \neq$ 0 , is the homogeneous representation for points $\left(x_{1} / x_{3}, x_{2} / x_{3}\right)$ in $\mathbb{R}^{2}$.

Now we discuss the case when $x_{3}=0$. The homogeneous representation for points in $\mathbb{R}^{2}$ with the form of $\left(x_{1}, x_{2}, 0\right)$ is known as ideal points, representing the points at infinity. If there are two parallel lines $(a, b, c)$ and $\left(a, b, c^{\prime}\right)$ in $\mathbb{R}^{3}$, the ideal point $(-b, a, 0)$ then lies on both of the two lines. Therefore, we can actually consider ideal point $\left(x_{1}, x_{2}, 0\right)$ as the intersection of two parallel lines in 3D world, which apparently extends to infinity. Based on the above discussions, we are now able to introduce the concept of vanishing points, as illustrated in Figure 2. Note that vanishing points are indeed the projection of ideal points on $\mathbb{P}^{2}$.

### 2.2 Projective transformation between texture image and scene image

The core idea for our texture re-rendering tool is to estimate the transformation between pixels in the texture image and pixels in the scene image, which is called texture mapping. And it is actually a projective planar transformation that maps one set of points in $\mathbb{P}^{2}$ to another set of points in $\mathbb{P}^{2}$. Figure 3 shows one instance of planar transformation from plane $\pi$ to plane $\pi^{\prime}$, and as is shown, point $x$ is mapped to point $x^{\prime}$. Now we are going to check the linearity of this transformation. As in Figure 3, $A B B^{\prime} A^{\prime}$ is a plane in 3D world that passes through center of projection


Figure 2. An illustration for projective geometry. Lines $A_{1} B_{1}, A_{2} B_{2}, C_{1} D_{1}$ and $C_{2} D_{2}$ are lines in $3 D$ world space. $A_{1} B_{1}$ is parallel to $C_{1} D_{1}$ while $A_{2} B_{2}$ is parallel to $C_{2} D_{2}$, also $A_{1} B_{1}$ is perpendicular to $A_{2} B_{2}$. $A_{1}^{\prime} B_{1}^{\prime}, C_{1}^{\prime} D_{1}^{\prime}, A_{2}^{\prime} B_{2}^{\prime}$ and $C_{2}^{\prime} D_{2}^{\prime}$ are respective projections on plane $\pi$. Note that $A_{1}^{\prime} B_{1}^{\prime}$ and $C_{1}^{\prime} D_{1}^{\prime}$ intersect at point $E_{1}^{\prime}$, while $A_{2}^{\prime} B_{2}^{\prime}$ and $C_{2}^{\prime} D_{2}^{\prime}$ intersect at point $E_{2}^{\prime}$. $E_{1}^{\prime}$ and $E_{2}^{\prime}$ are vanishing points in plane $\pi$. And these vanishing points correspond to orientations of lines in 3D world space.
$O$, plane $\pi$ and plane $\pi^{\prime}$, which intersects plane $\pi$ at line $A B$ and plane $\pi^{\prime}$ at line $A^{\prime} B^{\prime}$. Furthermore, line $A^{\prime} B^{\prime}$ is the mapping of line $A B$ from plane $\pi$ to plane $\pi^{\prime}$, thus lines in $\mathbb{P}^{2}$ are mapped to lines in $\mathbb{P}^{2}$. Therefore, the projective transformation between two lines in $\mathbb{P}^{2}$ is a linear transformation on homogeneous 3D vectors, and it indeed can be represented by a non-singular 3 by 3 homogeneous matrix $H$ [3]. In texture mapping, plane $\pi$ in Figure 3 is the texture image, and $\boldsymbol{x}$ represents one pixel in the texture image. Meanwhile, plane $\pi^{\prime}$ is the scene image that is to be re-rendered, and $\boldsymbol{x}^{\prime}$ represents one pixel in the scene image. Note that although $\boldsymbol{x}$ and $\boldsymbol{x}^{\prime}$ are both points in $\mathbb{P}^{2}$, we are using homogeneous representations. Therefore $\boldsymbol{x}$ and $\boldsymbol{x}^{\prime}$ are both 3D vectors. As a result, we denote $\boldsymbol{x}$ as $\left(x_{1}, x_{2}, x_{3}\right)^{\top}$ and vector $\boldsymbol{x}^{\prime}$ as $\left(x_{1}^{\prime}, x_{2}^{\prime}, x_{3}^{\prime}\right)^{\top}$. Then the transformation between vector $\boldsymbol{x}$ and $\boldsymbol{x}^{\prime}$ can be expressed as:

$$
\left(\begin{array}{l}
x_{1}^{\prime}  \tag{1}\\
x_{2}^{\prime} \\
x_{3}^{\prime}
\end{array}\right)=\left[\begin{array}{lll}
h_{11} & h_{12} & h_{13} \\
h_{21} & h_{22} & h_{23} \\
h_{31} & h_{32} & h_{33}
\end{array}\right]\left(\begin{array}{l}
x_{1} \\
x_{2} \\
x_{3}
\end{array}\right)
$$

Here we use $h_{i j}$ to represent $i$ th row and $j$ th column element of homogeneous matrix $H$.

### 2.3 Calculating entries of homogeneous transformation matrix $\mathbf{H}$

In Section 2.2, we discussed the homogeneous transformation matrix for mapping points between $\mathbb{P}^{2}$. The next step is how we calculate the elements in homogeneous matrix $H$. As is indicated in previous sections, we are given a set of points $\boldsymbol{x}$ represented by homogeneous 3D vectors in $\mathbb{P}^{2}$, and another set of points $\boldsymbol{x}^{\prime}$ in $\mathbb{P}^{2}$, which are also represented by homogeneous 3D vectors. The homogeneous matrix $H$ between $\mathbb{P}^{2}$ is then established such that $\boldsymbol{x}^{\prime}=\boldsymbol{H} \boldsymbol{x}$.

The first question is how many coordinate sets $\left(\boldsymbol{x}, \boldsymbol{x}^{\prime}\right)$ are needed for $H$ calculation. We notice that matrix $H$ has 9 entries, but the number of degrees of freedom for projective transformation between $\mathbb{P}^{2}$, is indeed 8 [3]. The reason is that suppose we


Figure 3. Projective transformation between two planes. $x_{0} y_{0} z_{0}$ is world coordinate frame, and its origin $O$ is the center of projection. $x$ is a point in plane $\pi$, and $x^{\prime}$ is a point in plane $\pi^{\prime}$. The mapping from plane $\pi$ to $\pi^{\prime}$ is a linear mapping $H$ between homogeneous coordinates such that $x^{\prime}=H \boldsymbol{x}$.
have two homogeneous matrices $H_{1}$ and $H_{2}$, where $H_{2}=a H_{1}$ and $a$ is a scalar, and then we apply projective transformation on same homogeneous 3D vector $\boldsymbol{x}$. According to Equation 1, we will get $x_{1}^{\prime}=H_{1} \boldsymbol{x}$ and $\boldsymbol{x}_{2}^{\prime}=H_{2} \boldsymbol{x}$. Since $H_{2}=a H_{1}$, we have $\boldsymbol{x}_{2}^{\prime}=a \boldsymbol{x}_{1}^{\prime}$. According to Section 2.1, we already know the fact that homogeneous 3D vectors $\boldsymbol{x}_{2}^{\prime}$ and $\boldsymbol{x}_{1}^{\prime}$ correspond to the same point in $\mathbb{P}^{2}$. Therefore, we can draw the conclusion that homogeneous matrices $H_{1}$ and $H_{2}$ indeed are the same projective transformation between points in $\mathbb{P}^{2}$. Finally, we are able to draw the conclusion that homogeneous matrix $H$ is defined up to a scalar, thus the 2D projective homogeneous transformation has 8 degrees of freedom.

Now we consider the way of calculating the entries' values for homogeneous transformation matrix $H$ using Direct Linear Transformation (DLT) algorithm [3]. Actually, we can infer the fact from Section 2.1 that 3D homogeneous representation $\left(x_{1}, x_{2}, x_{3}\right)$ for a point in $\mathbb{P}^{2}$ has 2 degrees of freedom. This is because $x_{3}$ just stands for an arbitrary none-zero ratio. Furthermore, we also infer from Section 2.2 that the degrees of freedom for point $\boldsymbol{x}$ must correspond to the degrees of freedom for its mapped point $H \boldsymbol{x}$. As a result, one coordinate mapping pair $(\boldsymbol{x}, H \boldsymbol{x})$ actually reduces the total degrees of freedom of the transform by 2. Therefore, in order to get efficient estimation for the entries of homogeneous transformation matrix $H$, it is necessary that we obtain 4 pairs of corresponding coordinate points to fully specify the matrix $H$. Now we set out to solve homogeneous matrix for our texture mapping method whereby it denotes the transformation from pixels of $\mathbb{P}^{2}$ in texture image to corresponding pixels of $\mathbb{P}^{2}$ in scene image. Note that here we are using homogeneous 3vectors for pixels in $\mathbb{P}^{2}$, as is explained in Section 2.1. Therefore, pixel ( $x_{1}, x_{2}$ ) in texture image is represented as:

$$
\boldsymbol{x}=\left(x_{1}, x_{2}, 1\right)^{\top}
$$

Similarly, pixel $\left(x_{1}^{\prime}, x_{2}^{\prime}\right)$ in scene image is represented as:

$$
\boldsymbol{x}^{\prime}=\left(x_{1}^{\prime}, x_{2}^{\prime}, 1\right)^{\top}
$$

Consequently, our texture mapping between $\boldsymbol{x}$ and $\boldsymbol{x}^{\prime}$ is the homogeneous transformation matrix $H$ such that

$$
\left(\begin{array}{c}
x_{1}^{\prime}  \tag{2}\\
x_{2}^{\prime} \\
1
\end{array}\right)=\left[\begin{array}{lll}
h_{1} & h_{2} & h_{3} \\
h_{4} & h_{5} & h_{6} \\
h_{7} & h_{8} & h_{9}
\end{array}\right]\left(\begin{array}{c}
x_{1} \\
x_{2} \\
1
\end{array}\right)
$$

where $h_{i}, i=1, \ldots, 9$ stands for the entries of matrix $H$. Now we use the denotation $\boldsymbol{h}^{i}$ to represent row vectors for matrix $H$, that is:

$$
\begin{aligned}
& \boldsymbol{h}^{1}=\left(h_{1}, h_{2}, h_{3}\right) \\
& \boldsymbol{h}^{2}=\left(h_{4}, h_{5}, h_{6}\right) \\
& \boldsymbol{h}^{3}=\left(h_{7}, h_{8}, h_{9}\right)
\end{aligned}
$$

Since $\boldsymbol{x}^{\prime}=H \boldsymbol{x}$, we infer that homogeneous vector $\boldsymbol{x}^{\prime}$ and $H \boldsymbol{x}$ are indeed in same direction. As a consequence, we know that:

$$
\begin{equation*}
\boldsymbol{x}^{\prime} \times H \boldsymbol{x}=\mathbf{0} \tag{3}
\end{equation*}
$$

where $\mathbf{0}=(0,0,0)^{\top}$, is the null 3D vector. And actually $H \boldsymbol{x}$ can be expanded as:

$$
H x=\left(\begin{array}{l}
h^{1} \cdot x \\
h^{2} \cdot x \\
h^{3} \cdot x
\end{array}\right)
$$

Therefore

$$
\begin{align*}
\boldsymbol{x}^{\prime} \times H \boldsymbol{x} & =\left(\begin{array}{c}
x_{1}^{\prime} \\
x_{2}^{\prime} \\
1
\end{array}\right) \times\left(\begin{array}{c}
\boldsymbol{h}^{1} \cdot \boldsymbol{x} \\
\boldsymbol{h}^{2} \cdot \boldsymbol{x} \\
\boldsymbol{h}^{3} \cdot \boldsymbol{x}
\end{array}\right)  \tag{4}\\
& =\left(\begin{array}{c}
x_{2}^{\prime} \boldsymbol{h}^{3} \cdot \boldsymbol{x}-\boldsymbol{h}^{2} \cdot \boldsymbol{x} \\
\boldsymbol{h}^{1} \cdot \boldsymbol{x}-x_{1}^{\prime} \boldsymbol{h}^{3} \cdot \boldsymbol{x} \\
x_{1}^{\prime} \boldsymbol{h}^{2} \cdot \boldsymbol{x}-x_{2}^{\prime} \boldsymbol{h}^{1} \cdot \boldsymbol{x}
\end{array}\right)=\mathbf{0}
\end{align*}
$$

Since:

$$
\boldsymbol{h}^{i} \cdot \boldsymbol{x}=\boldsymbol{x}^{\top} \cdot \boldsymbol{h}^{i \top}
$$

expressions in Equation 4 may actually be re-written as:

$$
\begin{align*}
\boldsymbol{x}^{\prime} \times H \boldsymbol{x} & =\left[\begin{array}{ccc}
\mathbf{0}^{\top} & -\boldsymbol{x}^{\top} & x_{2}^{\prime} \boldsymbol{x}^{\top} \\
\boldsymbol{x}^{\top} & \mathbf{0}^{\top} & -x_{1}^{\prime} \boldsymbol{x}^{\top} \\
-x_{2}^{\prime} \boldsymbol{x}^{\top} & x_{1}^{\prime} \boldsymbol{x}^{\top} & \mathbf{0}^{\top}
\end{array}\right]\left(\begin{array}{c}
\boldsymbol{h}^{1 \top} \\
\boldsymbol{h}^{2 \top} \\
\boldsymbol{h}^{3 \top}
\end{array}\right)  \tag{5}\\
& =L \boldsymbol{h}=\mathbf{0}
\end{align*}
$$

Note that here we have:

$$
\boldsymbol{h}=\left(\boldsymbol{h}^{1}, \boldsymbol{h}^{2}, \boldsymbol{h}^{3}\right)
$$

is a 9 -vector that is constituted by 9 entries of homogeneous matrix $H$. Furthermore, we notice the fact that if we left multiply matrix $L$ by two elementary matrices in Equation 5:

$$
L^{\prime}=\left[\begin{array}{rrr}
1 & 0 & 0 \\
0 & 1 & 0 \\
x_{1}^{\prime} & 0 & 1
\end{array}\right]\left[\begin{array}{rrr}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & x_{2}^{\prime} & 1
\end{array}\right] L
$$

we will end up getting

$$
\begin{align*}
L^{\prime} \boldsymbol{h} & =\left[\begin{array}{ccc}
\mathbf{0}^{\top} & -\boldsymbol{x}^{\top} & x_{2}^{\prime} \boldsymbol{x}^{\top} \\
\boldsymbol{x}^{\top} & \mathbf{0}^{\top} & -x_{1}^{\prime} \boldsymbol{x}^{\top} \\
\mathbf{0}^{\top} & \mathbf{0}^{\top} & \mathbf{0}^{\top}
\end{array}\right]\left(\begin{array}{c}
\boldsymbol{h}^{1 \top} \\
\boldsymbol{h}^{2 \top} \\
\boldsymbol{h}^{3 \top}
\end{array}\right)  \tag{6}\\
& =\mathbf{0}
\end{align*}
$$

As a consequence, we are able to reach the conclusion that Equation 5 actually give rise to 2 linearly-independent constraints for solving homogeneous transformation matrix $H$. At the beginning
of Section 2.3 we explained that in order to efficiently calculate $H$, it is necessary that four corresponding coordinate pairs $\left(\boldsymbol{x}_{i}, \boldsymbol{x}_{i}^{\prime}\right)$ are given, where $i=1,2,3,4$. And following the denotations in Section 2.3, we have $\boldsymbol{x}_{i}^{\prime}=\left(x_{1 i}^{\prime}, x_{2 i}^{\prime}, 1\right)$, where $\left(x_{1 i}^{\prime}, x_{2 i}^{\prime}\right), i=1,2,3,4$ are the pixel values in scene image, and $\boldsymbol{x}_{i}=\left(x_{1 i}, x_{2 i}, 1\right)$, where $\left(x_{1 i}, x_{2 i}\right), i=1,2,3,4$ are the pixel values in texture image. Consequently we will have 8 linear equations. And based on the result in Equation 6, the four equation sets for solving texture mapping matrix $H$ are expressed as:

$$
\left[\begin{array}{ccc}
\mathbf{0}^{\top} & -\boldsymbol{x}_{i}^{\top} & x_{2 i}^{\prime} \boldsymbol{x}_{i}^{\top}  \tag{7}\\
\boldsymbol{x}_{i}^{\top} & \mathbf{0}^{\top} & -x_{1 i}^{\prime} \boldsymbol{x}_{i}^{\top}
\end{array}\right]\left(\begin{array}{c}
\boldsymbol{h}^{1 \top} \\
\boldsymbol{h}^{2 \top} \\
\boldsymbol{h}^{3 \top}
\end{array}\right)=\mathbf{0}
$$

where $i=1,2,3,4$. Note that matrix $H$ is defined up to a scalar, and in homogeneous 3D vector $\left(x_{1}, x_{2}, x_{3}\right)$, component $x_{3}$ is actually the scaling factor, thus without loss of generality, we set $h_{9}=1$, in other words, $\boldsymbol{h}^{3}=\left(h_{7}, h_{8}, 1\right)$. Consequently, as denoted in Equation 2, we are able to calculate the remaining 8 entries $h_{j}$, where $j=1,2, \ldots, 8$ in texture mapping matrix $H$.

## 3. Methodology

### 3.1 User selection of 4 coordinates sets

In Section 2, we proved that in order to get the texture mapping matrix $H$, we need four corresponding pixel sets, separately from the texture image and the indoor scene image. Also we noticed in Figure 2 that different points $A, B, C, D$ on $\mathbb{P}^{2}$ may lead to different vanishing points, thus corresponding to different orientations in 3D world. As a result, an arbitrary user selection of the four coordinate sets from images may not lead to a proper texture mapping matrix that corresponds to indoor room geometry layout. Consequently, judging the room layout while selecting points from images is challenging for normal users, which is not what we want for a user-friendly interface. Hence in our method, we introduce a semi-automatic way to make it easy for users to select the reasonable coordinate sets from scene images and texture images.

The flow chart in Figure 4a illustrates an instance of how the user selects four pixels from the scene image. Firstly, the user


Figure 4. Flow charts that illustrate how the user selects four corresponding pixels from the scene image and the texture image. (a) From left to right: A click-based segmentation framework [4], a geometry layout estimation framework [2], a generated cubic hypothesis from scene image and a user-selected cuboid surface. (b) From left to right: A non-parametric texture synthesis framework [5] and a rectangular window in texture image.


Figure 5. Generating texture mapping matrix $H$, given four corresponding points in a texture image and a scene image. Through $H$, pixels at $\boldsymbol{x}_{i}$ are mapped to pixels at $\boldsymbol{x}_{i}^{\prime}$, for $i=1,2,3,4$.
interacts with our tool through a click-based segmentation framework for indoor scene images [4], which is capable of generating a mask for the components in indoor scene images onto which users would like to re-render new textures. In this case, a floor plane is picked out. Secondly, an embedded geometry layout estimation framework [2] is able to autonomously generate spatial estimation of room layout by presenting users parametrized cubic hypotheses that correspond to 3 primary orthogonal orientations of the room scene, as shown in Figure 4. In addition, each of the cuboid surfaces has the same orientation as a rectangular plane in world scene. In next step, the users is able to interact with our tool by selecting one of the surfaces from the generated cubic. Note that in Figure 4, the bottom surface of the cubic is selected, since it is corresponding to $z$ axis in room scene configuration, which matches the orientation of the selected floor plane. Once the cubic surface is selected, acquiring the four coordinates from scene image is straight-forward. They are indeed the pixel values on the four corners of the selected cuboid surface.

Next we are going to discuss how the user selects four pixels from the texture image. We already know that four pixels selected from the scene image corresponds to the orientation of a rectangular plane in the world scene. Thus it is quite straight-forward that a rectangular window on a texture image can be used to determine four pixels on the texture image. The flow chart in Figure 4 b illustrates an instance of selecting four pixels from a texture image. In the backend, an embedded texture synthesis framework [5] takes a small texture pattern as input and presents the user with a synthesized large texture pattern. Then the user is able to choose a rectangular window on the synthesized texture. Finally, the pixel values on the four corners of the rectangular window act as the four coordinates from texture image. After all four corresponding coordinate sets

$$
\left(\boldsymbol{x}_{i}, \boldsymbol{x}_{i}^{\prime}\right), i=1,2,3,4
$$

where $\boldsymbol{x}_{i}$ is the homogeneous 3 -vector representing pixels in the texture image and $\boldsymbol{x}_{i}^{\prime}$ is the homogeneous 3 -vector representing pixels in the scene image, are picked, by using Equation 7, we are able to generate texture mapping matrix $H$ (as shown in Figure 5). And then the tool is able to re-render the selected component (as in Figure 4a) with the new texture (as in Figure 4b).


Figure 6. Proposed methods for refining texture re-rendering results: (a) Cuboid surface shifting, the green surface is before shifting, and the purple surface is after shifting. The shifting direction, in this case, is along $-x$ axis. (b) Rectangular sampling window re-sizing, three yellow rectangular shapes corresponds to three sampling windows in texture image with different sizes. In this case, the window is expanding.

### 3.2 Re-rendering adjustments

In this section, we talk about adjusting re-rendering result. Using the texture mapping matrix generated from Section 3.1 can be useful enough if we only consider the re-rendering result correspondence with the indoor scene (room) geometry layout. Nevertheless, some re-rendering results may be visually over-sized and thus unfitted for some certain scene configurations (as shown in Figure 8b). Thus, there is necessity for our tool to propose approaches to refine texture re-rendering results through userinteractions. And Figure 6 shows our proposed two methods, which include cubic surface shifting in the scene image and sampling window re-sizing in the texture image. As is seen in Figure 6 a, the cubic surface before and after shifting has the same orientation (both perpendicular to $x$ axis). Meanwhile, the sampling windows with different sizes obviously have same orientation, since the texture image itself is a plane. Consequently, through the adjustment, the scaling of the re-rendering result is changing, while the orientation of the re-rendered texture, with respect to room geometry layout, is not changing. Hence users can interact with our texture re-rendering tool in either of the two ways to get a satisfying scaling effect for the re-rendering result.

### 3.3 High-resolution rendering

A critical case that we are especially interested in is to increase the re-rendering quality, while not increasing time consumption too much. Before our method, the contradictory point is that on one hand, for low resolution images, it is fast to generate cubic hypothesis (see Table 1), but the rendering quality is poor. The re-rendered texture may come with a bundle of artifacts which are certainly unwelcome by users. On the other hand, for high-resolution images, although it is time-consuming to generate cubic hypothesis (see Table 1), the rendering quality is satisfying. In practical cases, users can neither accept that it takes too long to get a result, nor that the rendering quality is of low-quality. Thus we propose a matrix scaling method that enables high-resolution images to utilize the texture mapping matrices generated from low-resolution images, for the purpose of re-rendering textures on high-resolution images while reduce time consumption for matrices generation.

Let us now think of a pair of two images. One image has a resolution $m \times n$ pixels and the other image has a higher resolution $a m \times$ an pixels $(a>1)$. Therefore, one pixel $\left(x_{0}, y_{0}\right)$ in the
low-resolution image corresponds to a pixel $\left(a x_{0}, a y_{0}\right)$ in the highresolution image. According to Section 2.1, the 3-vector homogeneous representations for $\left(x_{0}, y_{0}\right)$ and $\left(a x_{0}, a y_{0}\right)$ are $\boldsymbol{x}_{\text {Low_Res }}^{\prime}=$ $\left(x_{0}, y_{0}, 1\right)$ and $x_{\text {High_Res }}^{\prime}=\left(a x_{0}, a y_{0}, 1\right)$, respectively. It is easy to see that the transformation between these 2 points is

$$
\left(\begin{array}{c}
a x_{0}  \tag{8}\\
a y_{0} \\
1
\end{array}\right)=\left[\begin{array}{lll}
a & 0 & 0 \\
0 & a & 0 \\
0 & 0 & 1
\end{array}\right]\left(\begin{array}{c}
x_{0} \\
y_{0} \\
1
\end{array}\right)
$$

Now, our method takes the low resolution image as input, and then follows the routine described in Section 3.1 to generate the texture mapping matrix from a texture image to the lowresolution image, which is denoted as $H_{\text {Low_Res }}$. Then, in order to get the texture mapping matrix from the same texture image to the high-resolution image, denoted as $H_{\text {High_Res }}$, we follow the discussion in Section 2.2:

$$
\boldsymbol{x}_{\text {Low_Res }}^{\prime}=H_{\text {Low_Res }} \boldsymbol{x}
$$

and

$$
\boldsymbol{x}_{\text {High_Res }}^{\prime}=H_{\text {High_Res }^{x}}
$$

where $\boldsymbol{x}$ is 3 -vector homogeneous representation for pixels in texture image. By comparing Equation 8 and the above two relationships, we have

$$
H_{\text {High_Res }} \boldsymbol{x}=\left[\begin{array}{ccc}
a & 0 & 0  \tag{9}\\
0 & a & 0 \\
0 & 0 & 1
\end{array}\right] H_{\text {Low_Res } \boldsymbol{x}}
$$

We know that $\boldsymbol{x}$ actually corresponds to a pixel in texture image, thus it cannot be a null vector. Thus, a straight-forward solution for Equation 9 is

$$
H_{H_{i g h \_R e s}}=\left[\begin{array}{lll}
a & 0 & 0  \tag{10}\\
0 & a & 0 \\
0 & 0 & 1
\end{array}\right] H_{\text {Low_Res }}
$$

From Equation 10 we know that $H_{\text {High_Res }}$ can actually be acquired from $H_{\text {Low_Res }}$, just by left-multiplying $H_{\text {Low_Res }}$ with a scaling matrix. In this way, we can avoid estimating $H_{\text {High_Res }}$ in a time-consuming way.

## 4. Experimental Results

In order to test the efficiency of our texture re-rendering tool, we firstly did texture re-rendering on different room configurations to check whether the newly applied texture corresponds to room spatial layout. And then we tested the efficiency of our tool with respect to re-rendering adjustment. Finally, we compared the results between low-resolution and high-resolution images.

Figure 7 shows the indoor scene image re-mixing results for different room configurations. The appearance of re-rendered textures in Figures 7a, 7b, 7c, 7e, 7g and 7i look plausible, because they not only visually correspond to room spatial layout, but also present a harmonious visual effect when their scaling in sizes are compared with the objects nearby. The appearance of re-rendered textures in Figures 7d, 7f, 7h look reasonable in the sense of correspondence with room geometry orientation. However, the results in these figures are basically generated from raw texture mapping


Figure 7. Texture re-rendering and indoor scene image re-mixing results in various room layout configurations. (a) re-rendered floor with bricks texture. (b) re-rendered side wall with bricks texture. (c) re-rendered floor with carpet-like texture. (d) re-rendered floor with stone texture. (e) re-rendered accent wall with bricks texture. (f) re-rendered ceiling with tiles texture. (g) re-rendered accent wall with bricks texture. (h) re-rendered floor with tile texture. (i) re-rendered side wall with bricks texture.
matrix with less refinement and user adjustments. Therefore they present us an inharmonious visual effect when their sizes are compared with that of nearby objects. Nevertheless, scaling can be refined and adjusted through our user-interface that is introduced in Section 3.2.

Figure 8 actually shows how user interaction affects the scaling of re-rendering results. As the highlighted brick tiles sug-

Table I: Time consumption comparison for different approaches to generate texture mapping matrix, experiment performed in MATLAB ${ }^{\circledR}$

| Image in Figure 9 | Image size (in pixels $\times$ pixels) | Approach for generating texture mapping matrix | Time consumed for generating texture mapping matrix |
| :---: | :---: | :---: | :---: |
| a | $\begin{aligned} & 1024 \times \\ & 683 \end{aligned}$ | Geometry layout estimation [2] | ~5 secs |
| b | $\begin{aligned} & 3861 \times \\ & 2574 \end{aligned}$ | Geometry layout estimation [2] | $>20$ mins |
| C | $\begin{aligned} & 3861 \times \\ & 2574 \end{aligned}$ | Our pro- posed matrix scaling method | ~5 secs |



Figure 8. Illustration of re-rendering adjustment, the adjustments are introduced in Figure 6. We denote cuboid surface shifting distance as $d$ in pixel, and sampling window size as win_size in pixels $\times$ pixels. Green blocks are highlighted brick tiles. (a) User-selected component to be re-rendered. (b) Re-rendering result when $d=100$ and win_size $=800 \times 800$. (c) Re-rendering result when $d=100$ and win_size $=1400 \times 1400$. (d) Re-rendering result when $d=120$ and win_size $=1800 \times 1800$.
gest, re-rendering result in Figure 8 b is visually inharmonious because the brick tiles are oversized when compared with cabinet top edges. However, as is observed in Figures 8c and 8d, with the changes in cuboid surface shifting distance and the sampling window sizes, the scaling of the brick tiles also changes accordingly. We now discuss this in detail. As suggested by highlighted brick tiles, in Figure 8c, around 4 brick tiles are aligned with cabinet top edge. And in Figure 8d, around 6 brick tiles are aligned with cabinet top edge. So re-rendering results in Figures 8c and 8d are actually showing brick tile with different scaling in size. In addition, we notice the fact from Figure 8 that all the 3 different re-rendering results have the same geometry orientation, which visually corresponds to room layout.

Finally, we discuss the result for our proposed highresolution re-rendering method. In the process of generating the results in Figure 9, we are actually using the same synthesized texture image with resolution $5000 \times 5000$ pixels for both lowresolution scene images and high-resolution scene images. But as is shown in Figure 9, the quality of re-rendered texture on the low-resolution image is poor - a lot of artifacts are visually notice-


Figure 9. High-resolution texture re-rendering and Low-resolution rerendering with zoomed-in view. (a) Re-rendering result on $1024 \times 683$ pixels scene image. (b) and (c) Re-rendering result on $3861 \times 2574$ pixels scene image. (b) and (c) are different in the way of generating texture mapping matrix (see Table 1).
able; while the re-rendering quality on the high-resolution image is plausible. The critical point here for re-rendering on the highresolution image is that, although results in Figures 9b and 9c look very similar, the time consumed for generating these two results are quite different. As shown in Table 1, in order to generate the texture mapping matrix, time consumed for Figure 9 b is more than 20 minutes while for Figure 9c, it is around 5 seconds. The results indicates that using our proposed matrix scaling method greatly enhances the efficiency of re-rendering on high-resolution images.

## 5. Conclusion

In the paper we propose a novel tool for texture re-rendering and indoor scene image re-mixing. The tool is able to autonomously align newly rendered texture with room spatial layout. Also it provides users an interface for adjusting the scaling of the re-rendered texture in order to match with practical object sizes. In addition, our tool is capable of proving high-quality rendering result efficiently. In the future, we plan to research options to autonomously enable more realistic outcomes: one is to autonomously adjust the scaling of re-rendered texture, the other is to add light and shadow effects.

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