

Saliency-Based Band Selection For Spectral Image Visualization

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Abstract

In this paper, we introduce a new band selection approach for the color visualization of spectral images. Unlike traditional methods, we propose to make a selection out of a comparison of the saliency maps of the individual spectral channels. This allows to assess how different they are in terms of prominent features. A comparison metric based on Shannon's information theory at the second and third order is presented and results are subjectively and objectively compared to other dimensionality reduction techniques on three datasets, demonstrating the efficiency of the proposed approach.

Introduction

Spectral imagery consists of acquiring a scene at more than three different ranges of wavelengths, usually dozens. Since spectral display devices are yet rare, most of today's popular display hardware is based on the tri-stimulus paradigm [1]. Thus, in order to visualize spectral images, a dimensionality reduction step is required so that only three channels (Red, Green and Blue for example) can contain most of the visual information while easing interpretation by preserving natural colors and contrasts [2].

Tri-stimulus representation of multi/hyperspectral images for visualization is an active field of research that has been thoroughly investigated over the past decades. One of the most common approaches is probably the one referred to as "true color". It can basically be achieved in two different ways: one consists of selecting the bands at 700nm, 546.1nm and 435.8nm (or the closest) and mapping them to the three primaries: R,G and B, respectively. The other one uses the CMF-based band transformation [3] (each primary R,G and B is the result of a specific linear combination of spectral channels in the visible range of wavelengths). Even though it generally yields a natural visual rendering, this approach does not take the data itself into account at all, and thus noise, redundancy, etc. are not accurately handled.

Another very common approach for dimensionality reduction is Principal Components Analysis (PCA), which has been extensively used for visualization purposes. Tyo *et al.* [4], investigated PCA for N-to-3 dimensionality reduction into the HSV color space. An automatic method to find the origin of the HSV cone is also proposed in order to enhance the final color representation. Later, Tsagaris *et al.* [5] suggested to use the fact that the red, green and blue channels, as they are interpreted by the human eye, contain

some correlation, which is in contradiction to the underlying decorrelation engendered by PCA. For that reason, the authors proposed a constrained PCA-based technique in which the eigendecomposition of the correlation matrix is forced with non-zero elements in its non-diagonal elements. Several other PCA-based visualization techniques can be found in the literature [6, 7, 8].

In order to alleviate the computational burden of the traditional PCA, Jia *et al.* [9] proposed a correlation-based spectrum segmentation technique so that principal components are extracted from different segments and then used for visualization. Other segmented PCA approaches are investigated in [10] including equal subgroups, maximum energy and spectral-signature-based partitioning.

In [11], Du *et al.* compared seven feature extraction techniques in terms of class separability, including PCA, Independent Components Analysis (ICA) and Linear Discriminant Analysis (LDA). ICA has also been studied by Zhu *et al.* [12] for spectral image visualization. They used several spectrum segmentation techniques (equal subgroups, correlation coefficients and RGB-based) to extract the first IC in each segment. The use of different color spaces for mapping of the PCs or ICs has been investigated by Zhang *et al.* [13].

In [2, 14], Jacobson *et al.* presented a band transformation method allowing the CMF to be extended to the whole image spectrum, and not only to the visible part. They proposed a series of criteria to assess the quality of a spectral image visualization. Later, Cui *et al.* [15] proposed to derive the dimensionality reduction problem into a simple convex optimization problem. In their paper, class separability is considered and manipulations on the HSV cone allow for color adjustments on the visualization. More recently, we have proposed a method based on class-separability in the CIELAB space for improved spectral image visualization [16].

All the previously presented approaches are *band transformation* techniques inasmuch as they produce combinations of the original spectral channels to create an enhanced representative triplet. As stated earlier, the often mentioned drawback of this kind of approach is the loss of physical meaning attached to a channel. That is, if, initially, a spectral band is implicitly linked to a range of wavelengths, what can we tell about a combination of them? A particular case of *band transformation* is called *band selection* and consists of linearly combining the channels while constraining the weighting coefficients in the duet

$\{0,1\}$. In other words, the resulting triplet is a subset of the original dataset. By doing this, one preserves the underlying physical meaning of the spectral channels, thus allowing for an easier interpretation by the human end user.

In [17], Bajcsy investigated several supervised and unsupervised criteria for band selection, including entropy, spectral derivatives, contrast, etc. Many signal processing techniques have been applied to band selection: Constrained Energy Minimization (CEM) and Linear Constrained Minimum Variance (LCMV) [18], Orthogonal Subspace Projection (OSP) [19, 20] or the One-Bit Transform (1BT) [21]. Also information measures based on Shannon's theory of communication [22] have been proven to be very powerful in the identification of redundancy in high-dimensional datasets. Mutual information was first used for band selection by Conese *et al.* [23]. In [24] and [25], two metrics based on mutual information are introduced in the context of image fusion evaluation. They measure how much information is shared by the original and the reduced datasets. In [26], mutual information is used to measure the similarity of each band with an estimated ground truth. Hence, irrelevant bands for classification purpose are removed. In [27], a normalized mutual information is used for hierarchical spectrum segmentation. However, to the best of our knowledge, never has saliency analysis been used as a means for band-selection-based visualization. It is nonetheless a very relevant approach to evaluate the relative informative content of spectral channels and therefore useful in the context of dimensionality reduction.

Visual attention modeling is the study of the human visual interpretation of a given scene. In other words, which objects/features will first draw attention and why. This notion is closely linked to the analysis of saliency. Following early influential work by Treisman *et al.* [28] and Koch & Ullman [29], Itti *et al.* [30] proposed a general visual attention model allowing for the computation of so-called saliency maps, which purpose is to predict human gaze given a certain scene. This model involves center-surround comparisons and combinations of three main feature channels, namely colors, intensity and orientations. More recent work involve for instance the use of spectral residual analysis [31] or information theory [32].

In this paper, we propose a new strategy for the color display of spectral images. Our contributions are based on two main ideas: making use of saliency maps as a means to compare spectral channels as well as measuring third-order redundancy by means of a generalization of Shannon's mutual information called co-information [33]. Consequently, the following is organized as follows: a first section tackles the band selection algorithm by defining a metric called "Normalized Mutual Saliency" and explaining the band selection algorithm, while a second part presents and discusses the results obtained before the conclusion.

Saliency maps

From the literature, one can find several ways of computing a saliency map from a color image but one of the most influential work is the model by Itti *et al.* [30]. It is

also one of the simplest method and this is why we have decided to use it in this study. This model is based on the extraction of so-called conspicuity maps, depicting the prominence of every single pixel in terms of three different features: color, intensity and orientation (the latter being analyzed through 4 different angles). In the case of spectral channels, not only color is not involved, but, since each channel describes the same scene, the analysis of orientation conspicuity doesn't require more than one channel to be properly achieved. In the end, this step simply requires the computation of $N + 4$ conspicuity maps for the obtention of N saliency maps (N being the number of spectral channels), each one of them representing the informative content of an individual spectral channel. By depicting the locations of strong center-surround differences, the thusly obtained saliency maps are a powerful means to compare spectral channels and are consequently very suitable for band selection.

Channels comparison

One then has several possibilities to compare saliency maps, the most simple being a summation of pixelwise euclidean distances. In this study, we have focused on the use of information measures for they allow for a statistical comparison of random variables (population of pixels) while taking into account the relative spatial locations of pixels. Thus, we introduce a metric simply derived from Shannon's mutual information that we will refer to as "Normalized Mutual Saliency" (NMS) and which is defined as follows:

$$NMS(im_1; im_2) = \frac{I(s(im_1); s(im_2))}{H(s(im_1) + s(im_2))}$$

with im_1 and im_2 any two images of same spatial dimensions, $s(\cdot)$ an operator computing the saliency map of its input and $H(\cdot)$ and $I(\cdot; \cdot)$ being respectively the entropy and mutual information operators. The normalization is indeed necessary to allow for the metric to be non-relative, as it has been suggested for instance in [27].

Since we need three channels to create the final color composite, we also define the third order NMS , based on the Co-Information, as defined by Bell [33]:

$$CI(X; Y; Z) = H(X) + H(Y) + H(Z) - H(X; Y) - H(X; Z) - H(Y; Z) + H(X; Y; Z)$$

then:

$$NMS(im_1; im_2; im_3) = \frac{|CI(s(im_1); s(im_2); s(im_3))|}{H(s(im_1) + s(im_2) + s(im_3))}$$

Other generalizations of mutual information to higher orders have been proposed in the literature such as Watanabe's *total correlation* [34] which is defined as the difference between the sum of marginal entropies and the joint entropy of the set. However, the main drawback of total correlation is that it measures both second and third order, indiscriminately, while giving more weight to the second order. McGill [35] presented the *interaction information*, which is basically the same as co-information, simply with an opposite sign.

A particularly interesting property of co-information is that it can take both positive and negative values. In the "positive" case, one talks about redundancy, whereas in the case of negative values, one talks about synergy. Redundancies are foreseeable from lower orders while synergies only appear when the set of random variables are taken together. The synergy case appears when, for instance, $I(X; Y|Z) > I(X; Y)$ that is, when the knowledge of Z increases the dependency between X and Y . In order to explain this particular property, we consider a simple XOR cell with two binary inputs, X and Y and an output $Z = X \oplus Y$. If we consider the inputs as independent, the following stands true: $I(X; Y) = 0$. If we now introduce the knowledge of Z , we also introduce the underlying knowledge of the XOR relation linking the three variables. For instance, if we know that $Z = 0$, we can deduce that $X = Y$, and, by this, we increase the dependency between the inputs so that $I(X; Y|Z) > I(X; Y)$. In the case of spectral images, this principle remains true. The knowledge of one channel can increase the mutual information between the two others and, in that case, the smaller the co-information, the higher the shared information. Therefore, co-information must be as close to zero as possible in order to minimize the superfluous information.

Band selection

The band selection is performed by first finding the most dissimilar couple of channels. Instead of an exhaustive and computationally costly search, we propose to use an algorithm similar to the one used in [20]. A first B_1 channel is selected randomly and the one from which it is the most dissimilar (B_2) is sought among the others. The same procedure is used on B_2 to find B_3 , and so on until $B_i = B_{i-2}$. Algorithm 1 describes the procedure for an N -bands spectral image.

Algorithm 1 Band selection

```

i = 0; k = 1; iterations = 0;
randomly choose j ∈ [1..N];
while (i != k) and (iterations < 20) do
    find temp = argmink[NMS(Bj; Bk)]
    i ← j; j ← k; k ← temp;
    iterations++;
end while
find k = argmin [NMS(Bi; Bj; Bk)]
{R, G, B} ← sort({Bi, Bj, Bk}) by desc. wavelength

```

The maximum number of iteration should be set accordingly to N . For instance, for a 31-bands image, we have assumed that the algorithm can converge within 20 iterations.

Experiments

Datasets

For our experiments, we used three calibrated multispectral datasets, ranging in the visible spectrum (400-700 nm):

- "MacBeth" is the well-known MacBeth CC color cal-

ibration target. It contains 31 channels

- "Sarcophagus" is a 35 bands (400-740nm) multispectral image representing a portion of a 3rd century sarcophagus from the St Matthias abbey in Trier, Germany [36]. It was acquired by means of a 8 channels filter wheel camera ranging only in the visible spectrum (400-740nm). Reflectance was reconstructed by means of a supervised neural-network-based algorithm.
- "Mural" is a 35 bands (400-740nm) multispectral image of a 16th century mural painting from the Brömser Hof in Rudesheim, Germany, acquired with a rotating-wheel-based multispectral camera.

As a pre-processing step, bands with average reflectance value below 2% and those with low correlation (below 0.8) with their neighboring bands have been removed, as suggested in [37].

The main reason why we have chosen these scenes is because they all include a MacBeth CC target which facilitates the evaluation of color rendering.

Benchmarking methods

In order to evaluate the performances of our method, we have selected two other dimensionality reduction techniques for comparison.

- PCA_{hsv} is the traditional Principal Components Analysis of which components are mapped to the HSV color space ($PC1 \rightarrow V; PC2 \rightarrow S; PC3 \rightarrow H$).
- LP-based band selection has been proposed by Du *et al.* [20] and consists of progressively selecting bands by maximizing their respective orthogonality. Due to the high memory requirements of this method, a spatial subsampling of the data is necessary. According to Du *et al.*, the subsampling rate can be chosen as high as 1:100 (only 1% of the pixels are kept) without affecting the results. This rate has been applied in this study.

Results

Figure 1 depicts the resulting color visualization of all the images and for the three dimensionality reduction approaches: PCA, LP and NMS.

It can be seen that the PCA-based method gives the least appealing results, while LP and NMS give quite similar and "eye-satisfying" images. On the first dataset, one can notice that the white patch (bottom left) is whiter in the LP result, but still very discriminable from all the others in the NMS-based band selection. However, if we now look at the orange-yellow patch (second row, last one on the right), it is much more discriminable from the yellow one in the result by our method. Similar trends on the blue/violet patches allows us to assess that our dimensionality reduction method is the one conveying the more discriminative information (in a perceptual manner).

Furthermore, and in order to objectively compare the results, we chose to use the MacBeth CC target, present in each scene and to compare the $L^*a^*b^*$ values of a set

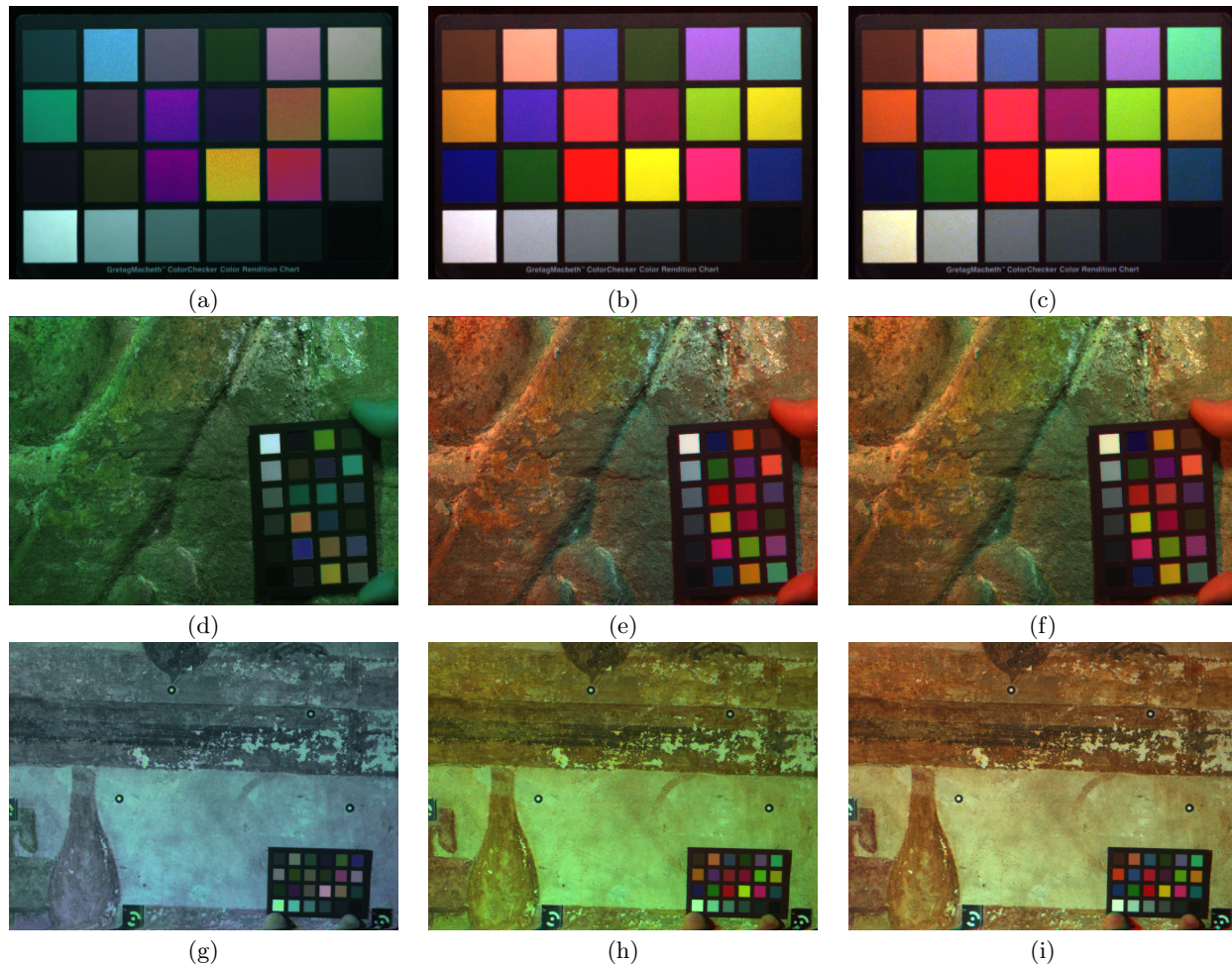


Figure 1. Different representations for each dataset (first column: PCA, second: LP and third: NMS)

of 480 manually selected pixels (20 by patch) with the "ground truth" ones, provided by Gretag, by means of the CIE76 ΔE_{ab^*} color difference metric. Dynamics of the color space components have been set as follows: $L^* \in [0..100]$, $a^* \in [-100..100]$ and $b^* \in [-100..100]$. With this framework, we aim at an assessment of how accurately the dimensionality reduction method can convey the high variety of colors from a high dimensional space to three dimensions. Table 1 gives the minimal, maximal and average perceptual distances in $L^*a^*b^*$ between the results and the "ground truth". It can be seen that, even though the LP-based band selection gives slightly better minimal and maximal errors in two cases, the proposed approach outperforms it on each dataset, in terms of average ΔE , and especially on the two last images.

Conclusion

We proposed a new band selection method based on saliency maps for the dimensionality reduction of spectral image. A simple metric based on information theory and called Normalized Mutual Saliency has been introduced and used as a means to compare spectral channels. Both second and third order versions of this metric have been

		PCA_{hsv}	LP	NMS
ΔE_{min}	"MacBeth"	8.55	3.36	3.80
	"Sarcophagus"	8.56	3.43	0.50
	"Mural"	8.38	5.95	2.30
ΔE_{max}	"MacBeth"	86.47	48.39	45.74
	"Sarcophagus"	80.42	38.16	38.60
	"Mural"	85.63	45.65	35.12
$\overline{\Delta E}$	"MacBeth"	32.30	29.17	28.95
	"Sarcophagus"	35.10	17.31	13.86
	"Mural"	46.76	19.93	15.42

Colorimetric errors

considered. Results on three different images have been subjectively and objectively assessed, proving the efficiency of the proposed method.

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